

MAT 119 – 002  
 Fall 2012  
 Review for Comprehensive Exam

Show all work.

The law of sines:  $\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$ .

One version of the law of cosines:  $a^2 = b^2 + c^2 - 2bc \cos A$ .

reference angle	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\pi$	$\frac{3\pi}{2}$
	0°	30°	45°	60°	90°	180°	270°
sin	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	0	-1
cos	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	-1	0
tan	0	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$	-	0	-

$$\sin 2x = 2 \sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$\sin \frac{x}{2} = \pm \sqrt{\frac{1 - \cos x}{2}}$$

$$\cos \frac{x}{2} = \pm \sqrt{\frac{1 + \cos x}{2}}$$



1. Find the domain of the function  $f(x) = \sqrt{x+2} + \sqrt{2-x}$ .

2. What changes need to be made to be made to the graph of  $y = 4^x$  to obtain the graph of  $y = 4^{x-3} + 1$ ?

3.  $f(x) = \sqrt{x-15}$  and  $g(x) = x^2 + 2x$ .

3a. Write  $g \circ f(x)$ .

3b. Find the domain of  $g \circ f(x)$ .

4.  $f(x) = \sqrt{3-x}$ ,  $x \leq 3$ . Find  $f^{-1}(x)$ .

\*5. Consider  $f(x) = \frac{2x^2 + 8x + 6}{x^2 - 2x}$ .

5a. Find the y-intercept.

5b. Find the x-intercept(s).

5c. Find the horizontal asymptote(s).

5d. Find the vertical asymptote(s).

6. Find the exact value of  $\cos(-225^\circ)$ .

7. Find the exact value of  $\cos\left(\frac{7\pi}{4}\right)$ .

8. Find the values of the six trigonometric functions of  $\theta$  from the information given:  $\cot\theta = \frac{3}{4}$  and  $\cos\theta < 0$ .

9. Solve the triangle with  $A = 48^\circ$ ,  $C = 57^\circ$ ,  $b = 47$ .

10. Solve the triangle with  $a = 90$ ,  $b = 70$ ,  $c = 40$ .

11. Find the amplitude, period, and phase shift of  $y = -3\sin\left(\frac{1}{2}x - \frac{\pi}{4}\right)$ .

12. Verify the identity  $\frac{1 + \sec x}{\sin x + \tan x} = \csc x$ .

\*13. Solve  $4\sin^2 x - 3 = 0$ .

14. Find the exact value  $\cos(112.5^\circ)$

15. Find the exact value of  $\sin^{-1}\left(\tan\frac{3\pi}{4}\right)$  without using a calculator.

16. Evaluate  $\log_2 128$ .

17. Evaluate  $e^{1+\ln 5}$ .

18. Rewrite as one logarithm:  $5\ln x - \frac{1}{2}\ln(3x-4) - 3\ln(5x+1)$ .

\*19. Solve for  $x$ :  $\log_3(3x) = \log_3 x + \log_3(4-x)$ .

\*20. Solve for  $x$ :  $e^{2x} + 2e^x - 15 = 0$ .