

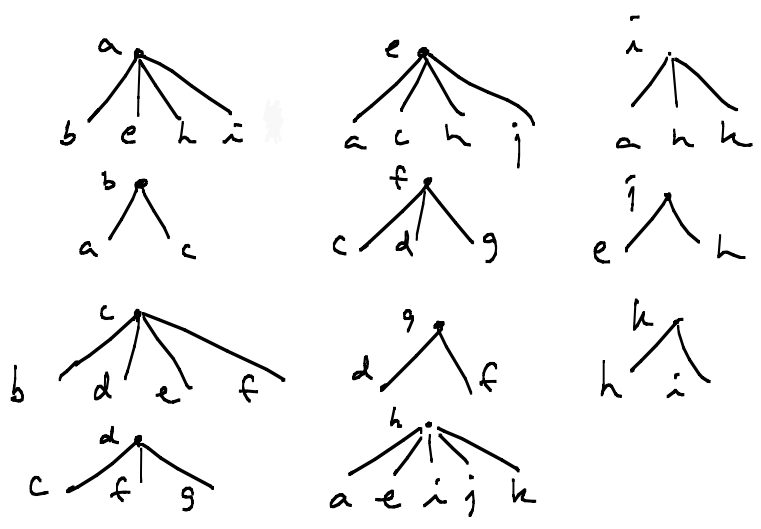


	order marked	recur. no.
a	1	
b	2	
c	3	
d	4	T
e	7	T
f	5	T
g	6	T
h	8	
i	9	T
j	11	
k	10	T

Depth first:  
a b c d f g e h i k j

break when 11 = # nodes appears

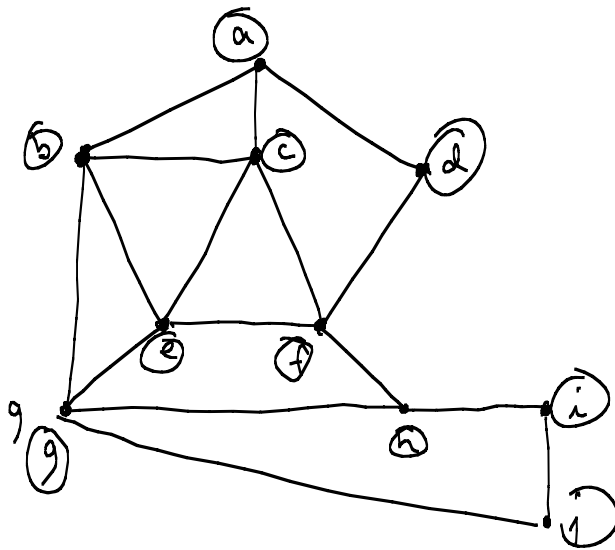
Now let's do breadth first:



Q	Pop	a
a	a	a
b	b	b
c	e	e
d	h	h
e	i	i
f	c	c
g	j	j
h	k	k
i	d	d
j	f	f
k	g	g

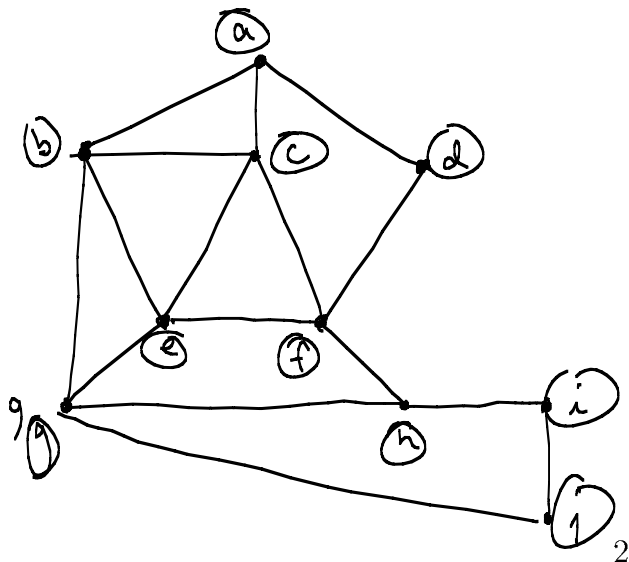
2. Find its neighbor nodes (ordering them lexicographically, again for sanity's sake!);
3. For each unmarked neighbor  $x$ , DepthFirst( $G, x$ )

Example: #3, p. 456/521



*d a b c e f h g j i*

Example: #5, p. 456/521



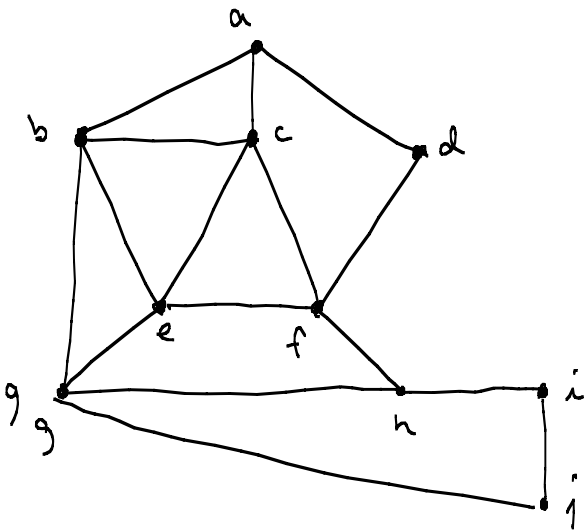
*e b a c f d h g j i*

## 1.2 Breadth-First

Examine the breadth-first algorithm on p. 450/516. It uses a queue to traverse the nodes, popping elements off the queue as all of their adjacent nodes are also marked.

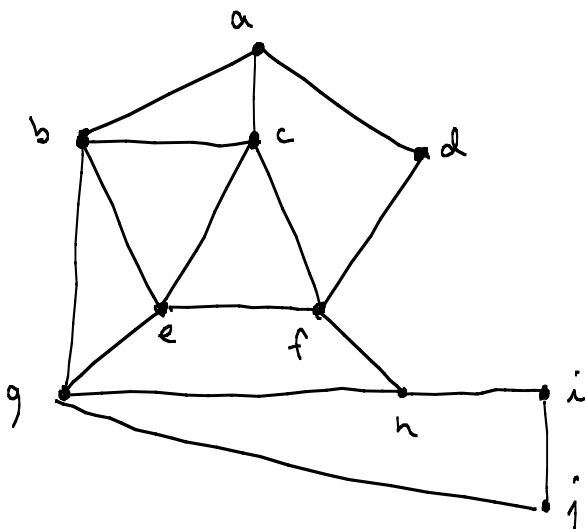
1. Pick (mark, write, and enqueue) the start node; then, while the queue is non-empty,
2. Find the front-of-the-queue's neighbor nodes (ordering them lexicographically to be kind);
3. Mark, write, and enqueue those which are as yet unmarked;
4. Dequeue the front element of the queue;
5. Continue until the queue is empty.

Example: #13, p. 457/522



d a f b c e h g i j  
 1 1 2 2 2 2 3 3 4

Example: #15, p. 457/522



## 2 How do these graph traversal algorithms behave for trees?

Look at an example (try a binary tree).

- Depth-first equates to preordering;
- Breadth-first does just what you'd expect! From the root on down, by depth.

## 3 Depth-First Application

These types of traversal algorithms are useful for operating on graphs. For example, I wrote some lisp code to find the shortest distance between two nodes  $x$  and  $y$ , using a depth-first algorithm (recursively). The algorithm is not particularly good; it was implemented because a student brainstormed it in a previous class, and it was a neat (albeit not particularly efficient) idea. It works like this:

- Start at the begin node;
- Find all adjacent nodes;
- Find the shortest distance from each of those nodes (recursively) to the destination node using a trimmed graph in which the start node has been eliminated (marked), and marking each one as finished once its shortest distance has been determined.

Note that I used the adjacency matrix representation, which is good for “full” graphs, but wasteful for sparse ones.

To test my algorithm, I ran it on the graph of Exercise #15, p. 444/510 for every pair of nodes (to compare the result with Floyd's algorithm). You can try out this procedure using this this web script:

<http://www.nku.edu/tidwell/melonga/cgi-bin/cgi-tcl-examples/generic/graph/graph.cgi>