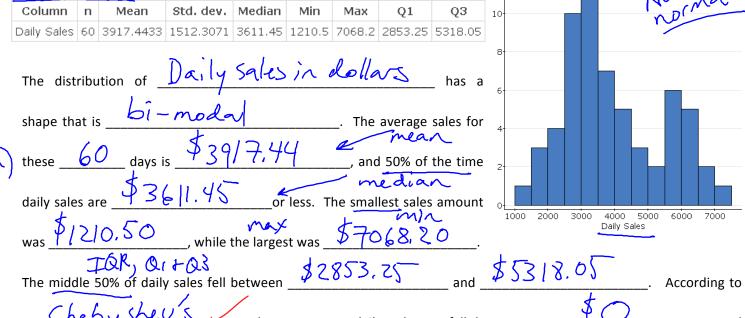
Packet 8: Sampling Distribution of the Sample Mean Textbook pages: 24 – 30; 701 After completing this material, you should be able to: explain what the symbols $\mu_{ar{\mathsf{v}}}$ and $\sigma_{ar{\mathsf{v}}}$ represent. describe the sampling distribution of the sample mean by discussing its shape, mean, and standard deviation. find probabilities associated with various sample means based on the sampling distribution. make inferences from the probability and explain the reasoning. A local pub is interested in learning more about their daily sales. In order to do this, daily sales (measured in dollars) from the past two months are collected. A histogram and summary statistics are given below. Use these to fill in the description of the distribution below – include units with the values where appropriate.

Frequency Summary statistics: Column Mean Std. dev. | Median Min 10



Cheby Sheu's Rule, we expect daily sales to fall between and \$8454,35 (three standard deviations from the mean)

Let's assume this is our population of sales values - what happens if we start to take samples of size 14 from this population of values?

Below is the sample which was taken – the values selected in the sample Frequency have been highlighted in pink on the original histogram.

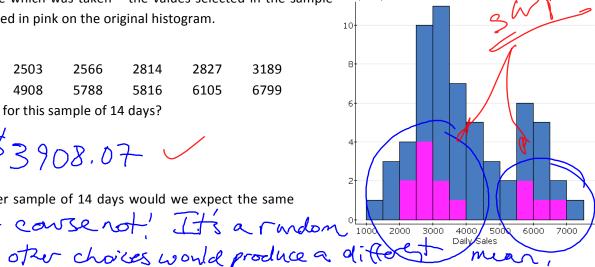
Sample Sales:

2062 2814 2827 2142 2503 2566 3189 3446 4908 5788 6105 6799 3748 5816

What is the mean for this sample of 14 days?

y=\$3908.07 ~

If we took another sample of 14 days would we expect the same consend! It's ar



Recall: What is a sampling distribution and why is it important? The sampling distribution	ry bage 2			
the distribution of a statistic obtained by samp	my -			
Recall: What is a sampling distribution and why is it important? The Sampling distribution of a startistic obtained by sampling this case, I the sampling distribution will be normal thanke dist. o	nore fy.			
We need to understand how the samples vary. To do this, we need to describe the sampling distribution of the sample mean. To do this, the following three characteristics must be addressed:				
· share - Welike nomality. If n > 30, w	e will			
· Shape - We like normality. If n > 30, w assume that the sampling dist, is no	ormal,			
· center - My = My = M m-mean of	/			
· spread - oy = or std. de n-sangle size	ev. of y			
bigger reduces spread of p	opulet.			
Example: Each of the following histograms represents a sampling distribution of the sample mean for various sample				
sizes. Samples of size 5, 15, and 40 were taken from some population. Match each histogram to the approp	oriate sample			
size. Mr must be around 20				
Frequency Frequency Frequency				
$\begin{array}{cccccccccccccccccccccccccccccccccccc$				
sample size: 40	whoch			
1/1	this of			
Based on the sampling distributions shown, what is the (approximate) population mean? Explain .	tich is			
m = 20 - all distributions are centred on 20 (orso).	hich.			
Centered on CO (orso).				
The population from which these samples were taken must have had what shape? Explain .				
These all look normal, even the sample of size S. So				
the distribution of y must have been pretty.	normal			
to begin with!				
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Example: It was reported that the average age for a Major League Baseball player is 27.2 years. With the end of the 2016 season, a sports enthusiast wants to know if the average age for players on the Cincinnati Reds is lower. To test this claim, a sample of 16 players on the Reds' roster will be taken. Assume the ages of all MLB players are normally distributed with a standard deviation of 3.12 years.

What variable will be recorded in the sample selected? Is this quantitative or categorical?

y-values — individual ages Only wire collecting 16 tomake 4.

Assign the appropriate notation to the values reported in the example.

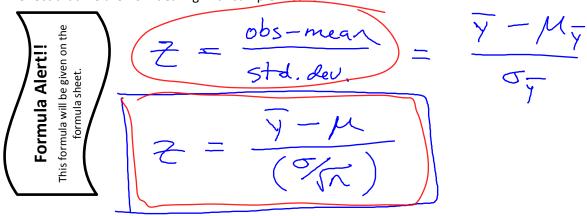
What conjecture has been made by the sports enthusiast?

The mean age of the sample obtained from Red's roster is less than 27.2 years : My

Describe the sampling distribution of the sample mean age which will be obtained from a sample of 16 players.

e - normal, since y is normally di My = M = 27.7 years

The fact that the sampling distribution of the sample mean is normally distributed is important – we know how to find probabilities from the normal distribution. To do this, though, we will need to modify our formula for the z-score to reflect that we are now dealing with sample means:



Let's go back to the example and see how this formula is used ...

	Back to the example: The sample of 16 players was taken and the average age was found to be 26.28 years. What is
_	the probability of observing this sample mean or some smaller value?
A,	A istreprobability of a value of z= 1.18 (or lower-more
	of 3= -1.18 (or lower-more
[Based on the probability found above, what conclusion can be drawn?
	While the result is to the left (y < M, so Z is
r J	regative), it is not extremely left: a value of 2 his extreme or more so occurs, 1190 of the time. So we
<u></u>	vould fail to reject a null of equality of Myth at any typical
r t	Example: According to Nielsen, the 2010 NCAA Men's Basketball Tournament (aka March Madness) averaged 10.19 million viewers (including online viewers). The NCAA has expanded its online coverage in recent years, and it is thought the mean number of viewers will have increased. Assume the population is right-skewed with a standard deviation of 5.15 million viewers. What conjecture has been made by the NCAA?
`	Rat te mean or will have increased due
5	to their expassive texceptional coverage.
	A sample of 40 tournament games is taken (from 2011 - 2014), completely describe the sampling distribution of the sample mean number of viewers? Y Shape: normal (n > 30) Rishribution of y (e.g. right) Skew
7	- center: $My = M = 10.19$ - spread: $Jy = Jh = 6.15/90 = .9724$ million Viewers The sample of 40 games has a mean of 11.76 million viewers. What is the probability of observing an average of 11.76
(y = 11.76 (good news! y > m - is it enough greater?)
	$z = \frac{y - M}{9\pi} = \frac{11.76 - 10.19}{.9724} = 1.61$
_	A-prob. of a value of 2 this greator greater = 19463
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Madness? A probability computed above, what can be concerned with the	
reject a null of squal me	ms (m= 10.19).
If the sample size were increased to 75 games, between what twee fall? The sample size were increased to 75 games, between what twee fall? The sample size were increased to 75 games, between what twee fall?	ited. Tie-off that we is a
	10.17 ± .71 : [9.48,10.90]
	10.17 ± .7 [9.48,10.90]
Example: An ambulance service reports that the mean time requirements with a standard deviation of 4.72 minutes. Given traffic that increased.	quired for ambulances to reach their destinations was 10
If a sample of 35 ambulance runs is selected, how would the destination be described?	he sampling distribution of the sample mean time to
-shape: with n = 30, expect y -center: My = M = 10	To occommend to
- Spread: 07 = 1 = 4172	= .778 minutes
Suppose that a sample of 35 ambulance runs is taken, and they minutes. What is the probability of observing a sample mean time and the sample mean time.	
21.5 Z= 5/R	
$= \frac{10.92 - 10}{.798}$	= :93 = 1,15 . of a = 12nt extreme or more so:
Based on the provability shove what (if anything) can be infe	erred about the mean time required for ambulances to
reach their destination? While y keas his We would get a result this his! I wouldn't feel confortable conclusions	thister 17.5 times out of a hundred. That mean time has increased.