

1 a. Mayans had a symbol indicative of the number zero that Babylonians did not have. ✓

b. Fish, fish, fish; fish, fish, fish was primarily shown to display the difference in primitive counting and modern arithmetic using one to one correspondence (in a sense) with words and fish vs. using addition.

Rock groups discusses similar counting styles as the Sesame Street character sort of made a rectangle with his words (fish fish fish fish fish fish) and groups of rocks can be used to show numbers as prime or composite depending on whether they can be formed into some form of rectangle or have to be a straight line.

c. Yanghui's triangle was first and is the same as Pascal's triangle (rows equal powers of 2, second diagonal being counting numbers etc.) but Yanghui's uses bamboo sticks while Pascal's uses our standard Hindu-Arabic notation.

d. Struaz regards Roman numerals as something along the lines of needlessly extravagant and time consuming compared to other counting systems.

e. skip

No place value ✓

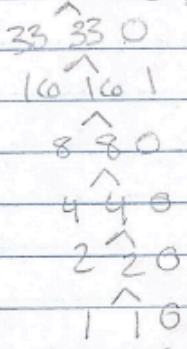
Problem 1:

- a. The Mayans had the number zero and the Babylonians did not.
- b. The point was instead of saying "fish, fish, fish, fish, fish, fish" it's much more easier and effective to say "6 fish." Rock groups demonstrated this as we can group rocks together into squares ^{rectangles} to determine if a number is prime or not. For example odd #'s make a 'L' shape whereas even #'s such as 6, 8, or 10 make squares. $\rightarrow \begin{matrix} \bullet & \bullet & \bullet \\ \bullet & & \bullet \\ \bullet & & \bullet \end{matrix}, \begin{matrix} \bullet & \bullet & \bullet & \bullet \\ \bullet & & \bullet & \bullet \\ \bullet & & \bullet & \bullet \\ \bullet & & \bullet & \bullet \end{matrix}, \begin{matrix} \bullet & \bullet & \bullet & \bullet & \bullet \\ \bullet & & \bullet & \bullet & \bullet \\ \bullet & & \bullet & \bullet & \bullet \\ \bullet & & \bullet & \bullet & \bullet \end{matrix}$
- c. Yanghui's was earlier, but was an earlier representation of Pascal's triangle. It was a Chinese Pascal's triangle.
- d. SKIP
- e. Pebbles & tallies. Pebbles were used as a one-to-one correspondence for counting sheep. One pebble equaled one sheep. If a sheep died, subtract a pebble, if a sheep was born, add a pebble. A second one was tallies. This was used for accounting or even things such as selling bread. A baker and a woman would each have a stick. Each time the baker sold a loaf, his stick and her stick would get a tally. At the end of the week they would compare tallies and she would pay for the ^{# of} loaves she bought based on the tallies.

© The ancient systems used one to one correspondence. 2 examples would be the shepherd and the pouch of pebbles and the tally sticks. The shepherd would count his sheep by having one pebble represent one rock (if one is lost/dies, a rock is thrown out; for a birth, one is added). The tally stick is a stick that used notches in order to count, like the baker and customer putting the same notches to keep track of their purchases.

2. a. 66 (1,0,0,0,0,1,0)

multi's

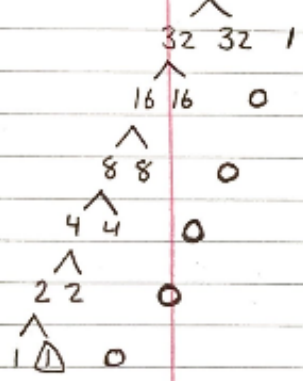


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b. 66 → 55 + 8 + 3 I would take 3 because the lowest fibonacci used to add to 66 is 3.

Problem 2: 65

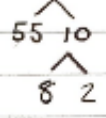
a. 65



1000001

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b. 65



2 counters because it is the lowest fibonacci number the 65 is broken down to

3 a. The idea of one-to-one correspondance is that one of an object is indicative of one of another object such as using 7 of my fingers to represent each of the 7 sheep I own.

3 b. Uniqueness is vital to the Binary card trick as the trick only works because every number is a unique sum of powers of 2 and that uniqueness is what allows Fraudini to quickly know a number after adding the powers of 2 on each card the person's number is present on.

Good description

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Problem 4:

Babylonian

Mayan

60

$$\frac{P}{60'} \quad \frac{60''}{60''}$$

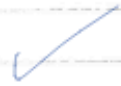


$$\frac{60}{20 \cdot 3 \cdot 0}$$



360

$$\frac{360}{PPP} \quad \frac{60''}{60''}$$



$$\frac{360}{}$$



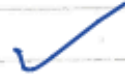
6124

$$\frac{6124}{3600} = \frac{4P}{60^2} + \frac{44PP}{60'} + \frac{PP}{60''}$$

2524



$$\frac{6124}{360 \cdot 17}$$



51761

$$\frac{51761}{41} = \frac{4PP}{60^2} + \frac{44PP}{60'} + \frac{44P}{60''}$$

14 22



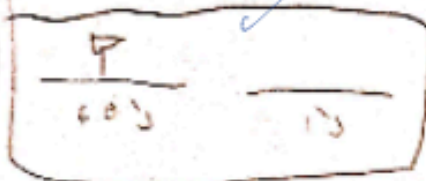

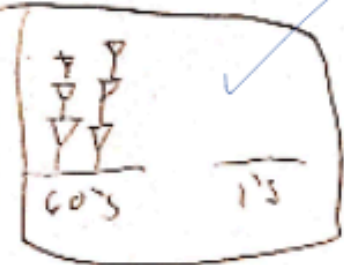

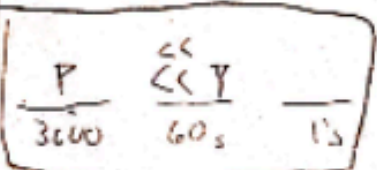

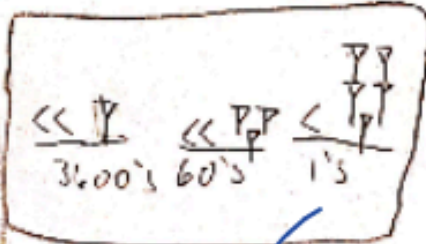
$$\frac{51761}{41} = \frac{50400}{7 \cdot 7200} + \frac{1361}{3 \cdot 360} + \frac{1690}{281 \cdot 280} + \frac{2014}{2014} + \frac{1}{1}$$



$$\begin{array}{r} 51761 \\ -50400 \\ \hline 1361 \\ -1320 \\ \hline 41 \end{array}$$

4.

(20)

Number	Baby Ionian	Mayan
60	$60 \leftarrow \begin{matrix} 60 \cdot 1 \\ 0 \end{matrix}$ 	$60 \leftarrow \begin{matrix} (20 \cdot 3) \\ 0 \end{matrix}$ 
360	$360 \leftarrow \begin{matrix} 60 \cdot 6 \\ 0 \end{matrix}$ 	$360 \leftarrow \begin{matrix} 300 \cdot 1 \\ 0 \end{matrix}$ 
6060	$6060 \leftarrow \begin{matrix} 6060 \\ / \backslash \\ 3600 \ 2400 \\ / \backslash \\ 60 \ 40 \end{matrix}$ 	$6060 \leftarrow \begin{matrix} 6060 \\ / \backslash \\ 3600 \ 2400 \\ / \backslash \\ 60 \ 40 \end{matrix}$ 
76995	$76995 \leftarrow \begin{matrix} 3600 \cdot 21 \\ 1395 \leftarrow 60 \cdot 23 \\ 15 \cdot 1 \end{matrix}$ 	$76995 \leftarrow \begin{matrix} (2200 \cdot 10) 4995 \\ (10 \cdot 360) 315 \\ (15 \cdot 20) 15 \end{matrix}$ 