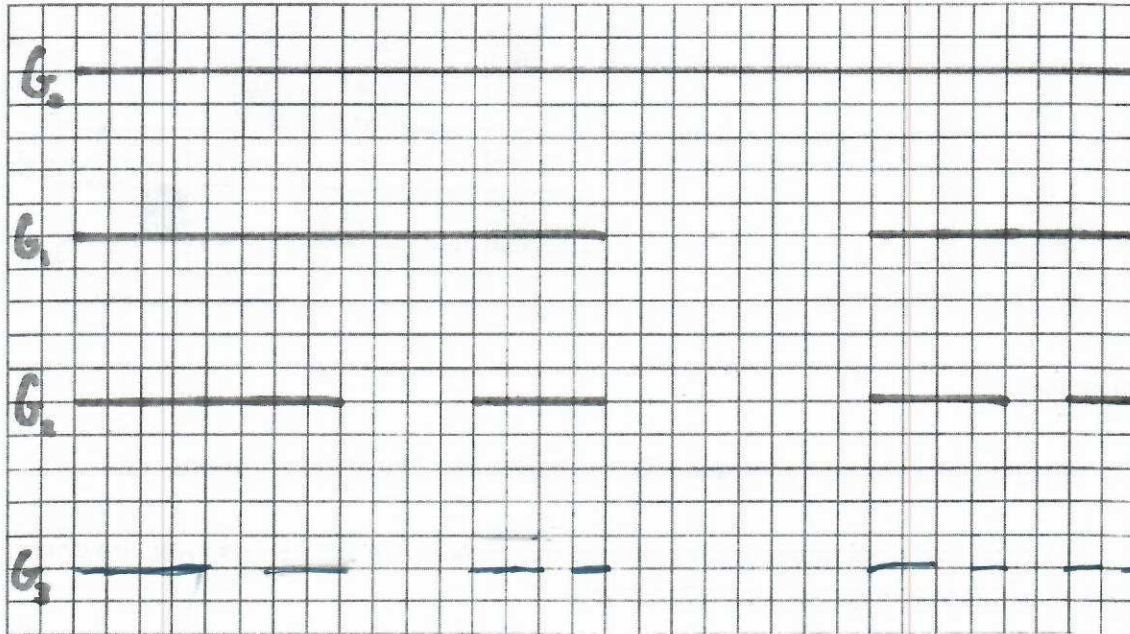


Quiz 09, MAT115, Spring 2024

Name:

Problem 1: In this case we have a stick fractal. The initiator is a stick; and we divide it into two sticks: one a quarter of the length of the original, and the other one half the length of the original stick.



Questions:

a. (2 pts) The initial stick we call generation 0, and the generator transforms it into generation 1. Do it again, and you reach generation 2. Draw generation 3.

b. (2 pts) A stick is divided into more sticks. How many sticks appear in generations 3, 4, and 5?

Nice work!

$$G_0 = 1 = 2^0$$
$$G_1 = 2 = 2^1$$
$$G_2 = 4 = 2^2$$

$$G_3 = 8 = 2^3$$
$$G_4 = 16 = 2^4$$
$$G_5 = 32 = 2^5$$

✓

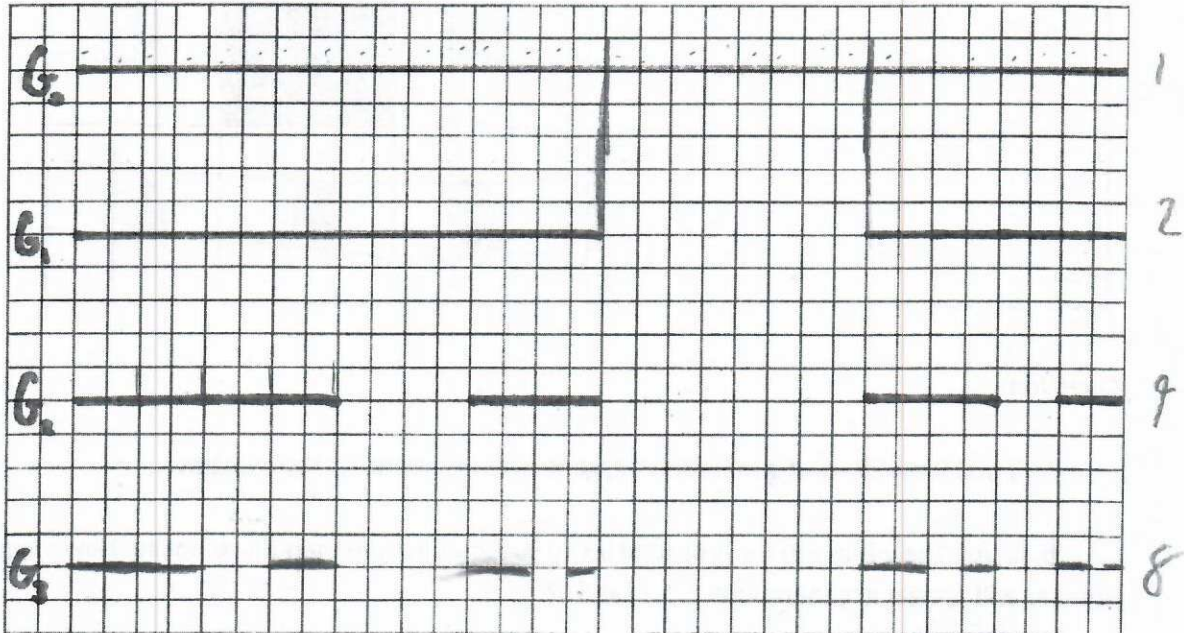
c. (1 pt) The initial stick has length equal to one unit. How much length is left in generation 1, after the first part is removed? How much length is left in generations 2, 3, 4, and 5?

$$G_1 = 3/4$$
$$G_2 = 9/16$$
$$G_3 = 27/64$$

$$G_4 = 81/256$$
$$G_5 = 243/1024$$

✓

Problem 1: In this case we have a stick fractal. The initiator is a stick; and we divide it into two sticks: one a quarter of the length of the original, and the other one half the length of the original stick.



Questions:

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b. (2 pts) A stick is divided into more sticks. How many sticks appear in generations 3, 4, and 5?

G_3 : 8 sticks
 G_4 : 16 sticks
 G_5 : 32 sticks

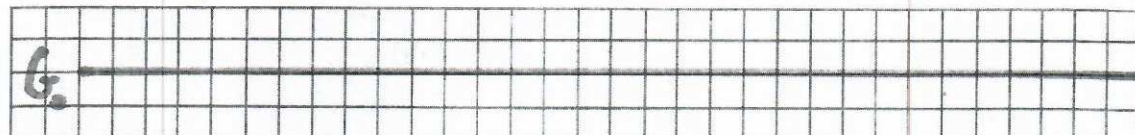
c. (1 pt) The initial stick has length equal to one unit. How much length is left in generation 1, after the first part is removed? How much length is left in generations 2, 3, 4, and 5?

$(3/4)^1 G_1: 0.75$
 $(3/4)^2 G_2: 0.5625$
 $(3/4)^3 G_3: 0.4219$
 $(3/4)^4 G_4: 0.3164$
 $(3/4)^5 G_5: 0.2373$

Nice!

Problem 1: In this case we have a stick fractal. The initiator is a stick; and we divide it into two sticks: one a quarter of the length of the original, and the other one half the length of the original stick.

$(2)^0$



$(\frac{3}{4})^0 = 1$

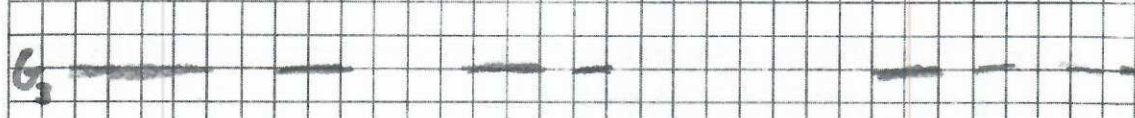
$(2)^1$



$(2)^2$



$(2)^3$



Questions:

$(2)^4$
 $(2)^5$

a. (2 pts) The initial stick we call generation 0, and the generator transforms it into generation 1. Do it again, and you reach generation 2. Draw generation 3.

b. (2 pts) A stick is divided into more sticks. How many sticks appear in generations 3, 4, and 5?

$3^0 \cdot (2)^3 = 8$

$4 \cdot (2)^4 = 16$

$5 \cdot (2)^5 = 32$



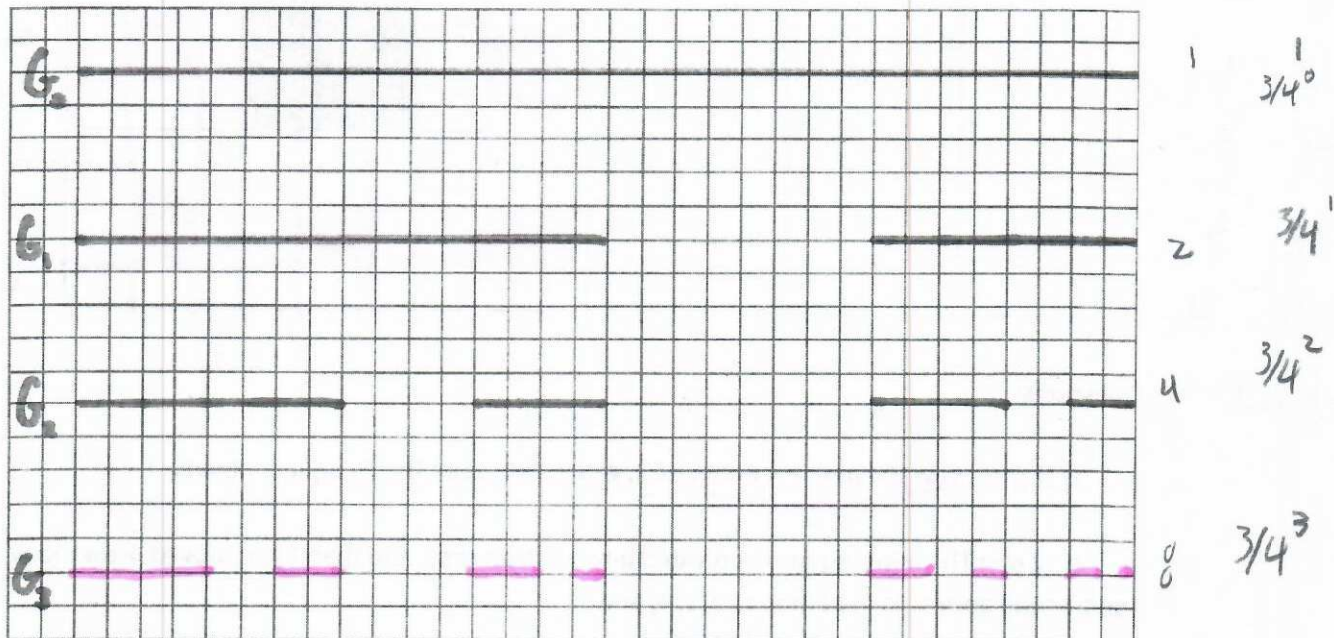
c. (1 pt) The initial stick has length equal to one unit. How much length is left in generation 1, after the first part is removed? How much length is left in generations 2, 3, 4, and 5?

$L_{G0} = (\frac{3}{4})^0 = 1$
 $L_{G1} = (\frac{3}{4})^1 = \frac{3}{4}$
 $L_{G2} = (\frac{3}{4})^2 = \frac{9}{16}$

$L_{G3} = (\frac{3}{4})^3 = \frac{27}{64}$
 $L_{G4} = (\frac{3}{4})^4 = \frac{81}{256}$
 $L_{G5} = (\frac{3}{4})^5 = \frac{243}{1024}$

Nice work!

Problem 1: In this case we have a stick fractal. The initiator is a stick; and we divide it into two sticks: one a quarter of the length of the original, and the other one half the length of the original stick.



Questions:

a. (2 pts) The initial stick we call generation 0, and the generator transforms it into generation 1. Do it again, and you reach generation 2. Draw generation 3.

b. (2 pts) A stick is divided into more sticks. How many sticks appear in generations 3, 4, and 5?

G_3 has 8 sticks, G_4 would have 16 sticks, and G_5 would have 32 sticks.

c. (1 pt) The initial stick has length equal to one unit. How much length is left in generation 1, after the first part is removed? How much length is left in generations 2, 3, 4, and 5?

In G_1 there is $\frac{3}{4}$ of the length left. (0.75)

In G_2 , there is $\frac{3}{4}^2$ length left. (0.5625)

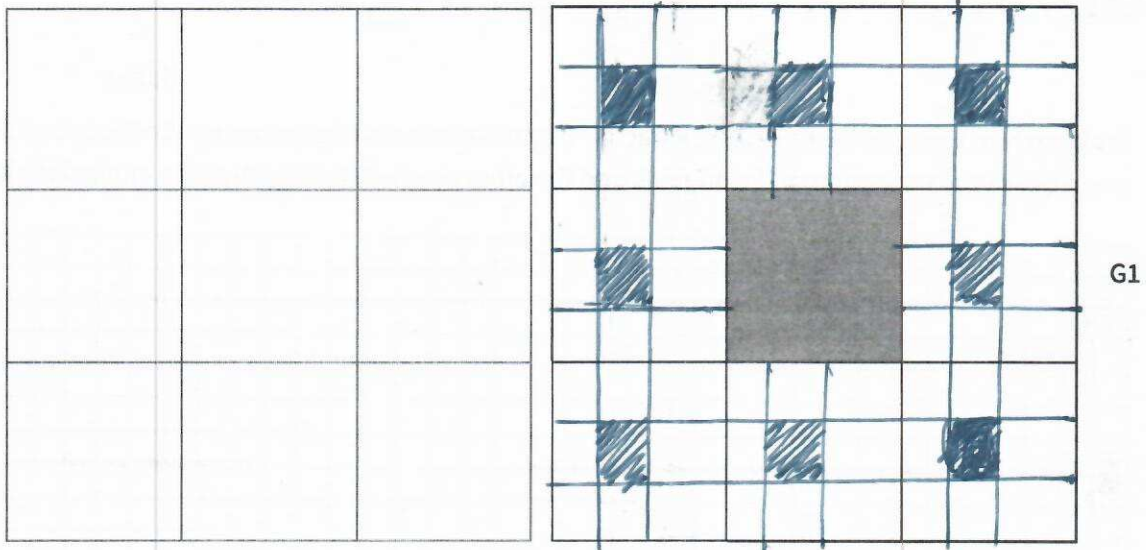
In G_3 , there's $\frac{3}{4}^3$ left. (0.421875)

In G_4 , there's $\frac{3}{4}^4$ left. (0.31640625)

In G_5 , there's $\frac{3}{4}^5$ left. (0.2373046875)

Nice
work

Problem 2: In this case we have an area fractal. The initiator is a square; and we divide it into 9 squares, and remove the middle square, as shown in these images. Now we can "do it again!"



Questions:

a. (2 pts) Draw the next generation G2, generation 2, on the G1 square above.

b. (2 pts) The initial square is divided into 9 subsquares, and then 1 is removed. How many squares will appear in generations 2, 3, 4, and 5?

$$\begin{aligned} G_0 &= 1 \\ G_1 &= 8 \\ G_2 &= 64 \end{aligned}$$

$$\begin{aligned} G_3 &= 512 \\ G_4 &= 4096 \\ G_5 &= 32768 \end{aligned}$$

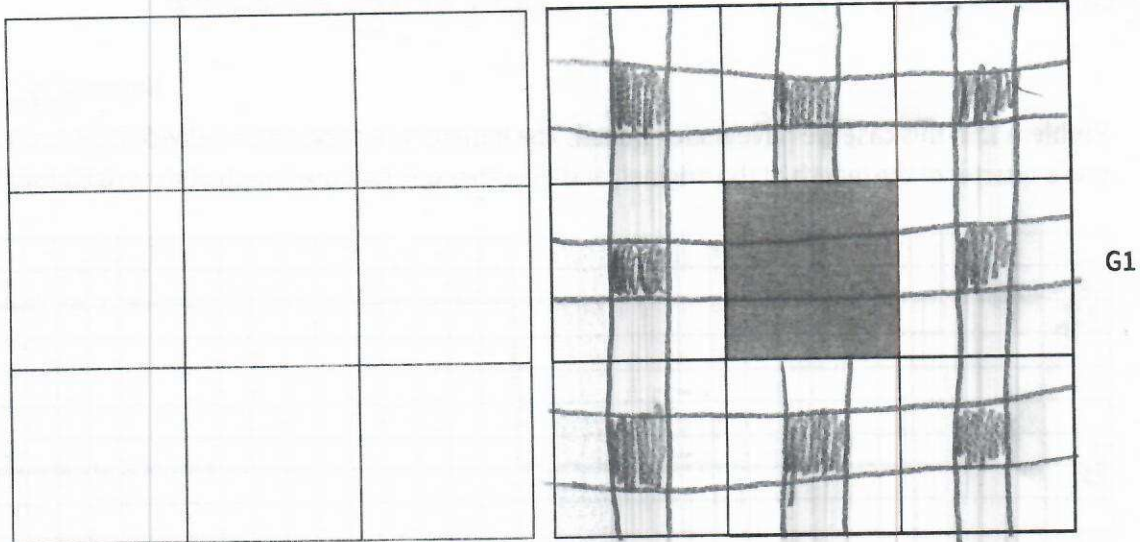
b. (1 pt) The initial square has area equal to one unit. How much area is left in generation 1, after the first square is removed? How much area is left in generations 2, 3, 4, and 5?

$$\begin{aligned} G_0 &= 1 \\ G_1 &= 8/9 \\ G_2 &= 64/81 \end{aligned}$$

$$\begin{aligned} G_3 &= 512/729 \\ G_4 &= 4096/6561 \\ G_5 &= 32,768/59,049 \end{aligned}$$



Problem 2: In this case we have an area fractal. The initiator is a square; and we divide it into 9 squares, and remove the middle square, as shown in these images. Now we can "do it again!"



Questions:

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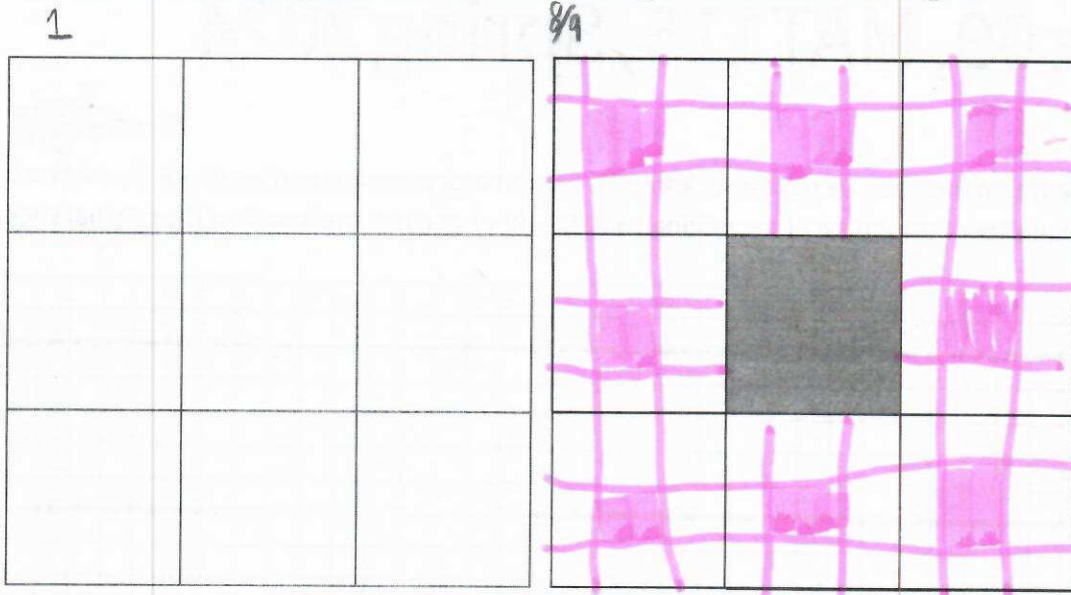
$$\begin{aligned}
 6^1 &= 8 \\
 6^2 &= 64 \\
 6^3 &= 512 \\
 6^4 &= 4,096 \\
 6^5 &= 32,768
 \end{aligned}$$

b. (1 pt) The initial square has area equal to one unit. How much area is left in generation 1, after the first square is removed? How much area is left in generations 2, 3, 4, and 5?

$$\begin{aligned}
 (8/9)^1 &= 0.8 \\
 (8/9)^2 &= 0.7901 \\
 (8/9)^3 &= 0.7023 \\
 (8/9)^4 &= 0.6243 \\
 (8/9)^5 &= 0.5549
 \end{aligned}$$

Problem 2: In this case we have an area fractal. The initiator is a square; and we divide it into 9 squares, and remove the middle square, as shown in these images. Now we can "do it again!"

9 0
 8 1
 64 2
 512 3
 4096 4
 32768 5



$G_0 = 1$
 $G_1 = 8/9$
 $G_2 = 64/9^2$
 $G_3 = 512/9^3$
 $G_4 = 4096/9^4$
 $G_5 = 32768/9^5$

Questions:

a. (2 pts) Draw the next generation G_2 , generation 2, on the G_1 square above.

b. (2 pts) The initial square is divided into 9 subsquares, and then 1 is removed. How many squares will appear in generations 2, 3, 4, and 5?

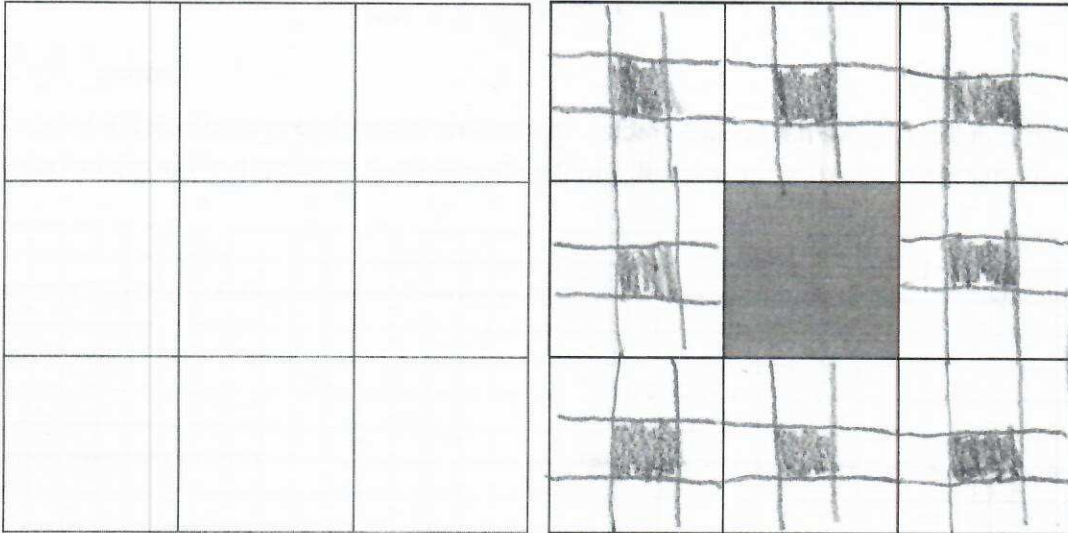
G_2 will be 64 squares
 G_3 will be 512 squares
 G_4 will be 4096 squares
 G_5 will be 32768 squares

b. (1 pt) The initial square has area equal to one unit. How much area is left in generation 1, after the first square is removed? How much area is left in generations 2, 3, 4, and 5?

In G_1 there is $8/9$ area left.
 In G_2 there is $8/9^2$ left. ($64/81$)
 In G_3 there's $8/9^3$ left.
 In G_4 there's $8/9^4$ left.
 In G_5 there's $8/9^5$ left

Problem 2: In this case we have an area fractal. The initiator is a square; and we divide it into 9 squares, and remove the middle square, as shown in these images. Now we can "do it again!"

G0
 $\left(\frac{8}{9}\right)^0 = 1$
 $(8)^0 = 1$



G1
 $\left(\frac{8}{9}\right)^1 = \frac{8}{9}$
 $(8)^1 = 8$

Questions:

a. (2 pts) Draw the next generation G2, generation 2, on the G1 square above.

b. (2 pts) The initial square is divided into 9 subsquares, and then 1 is removed. How many squares will appear in generations 2, 3, 4, and 5?

$2 = 8^2 = 64$ $5 = 8^5 = 32,768$
 $3 = 8^3 = 512$
 $4 = 8^4 = 41,088$

b. (1 pt) The initial square has area equal to one unit. How much area is left in generation 1, after the first square is removed? How much area is left in generations 2, 3, 4, and 5?

$G0 = \left(\frac{8}{9}\right)^0 = 1$ $G3 = \left(\frac{8}{9}\right)^3 = \frac{512}{729}$
 $G1 = \left(\frac{8}{9}\right)^1 = \frac{8}{9}$ $G4 = \left(\frac{8}{9}\right)^4 = \frac{4096}{6561}$
 $G2 = \left(\frac{8}{9}\right)^2 = \frac{64}{81}$ $G5 = \left(\frac{8}{9}\right)^5 = \frac{32,768}{59,049}$

good!