Packet 11: Two Sample Inferences for the Mean After completing this material, you should be able to: identify whether two samples are independent or dependent. conduct a hypothesis test for the mean difference (μ_d) when dependent samples are taken. calculate a confidence interval estimating the mean difference (μ_d) when dependent samples are taken. conduct a hypothesis test for the difference in the means $(\mu_1 - \mu_2)$ when independent samples are taken. calculate confidence interval estimating the difference in the means $(\mu_1 - \mu_2)$ when independent samples are To celebrate the Cubs winning the World Series ... a baseball enthusiast wants to compare the mean batting average for the Chicago Cubs & the Cleveland Indians. What variable will be recorded for the sampled players? Is the variable quantitative or categorical? Batting Averages - qualitative To make the comparison, he needs to gather 2016 batting averages from members of each team. This can be done using one of the following two scenarios: Scenario 1: The individual samples 5 players from the Scenario 2: The individual randomly samples 5 Cubs' roster and records each player's batting positions in the line-up from 9 possible and records average. Then, he samples 5 players from the Indians' the batting average for the player batting in that

Cubs' roster and records each player's batting average. Then, he samples 5 players from the Indians' roster and records each player's batting average.

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In both sampling scenarios described, the sports enthusiast ends up with 5 batting averages for the Cubs and 5 batting averages for the Indians. But, the way in which these samples were taken were fundamentally different. One scenario employed the use of *dependent* (or paired) samples, while the other used *independent* samples. Let's define these two sampling techniques:

Dependent samples: Paired samples is that obs. with in sample I match the obs. units in sample I in some important of relevant way (we "control" for a variable ").

Independent samples: Ungained samples: no attempt is made to
pair or relate individual observational units across the
two samples.

Let's look at additional examples and determine the type of sample selected:

Example 1: Three hundred registered voters were selected at random to participate in a study on attitudes about how well the president is performing his job. They were each asked to answer a short multiple-choice questionnaire and then they watched a 20-minute video that presented information about the job description of the president. After watching the video, the same 300 selected voters were asked to answer a follow-up multiple-choice questionnaire. The investigator of this study will have two sets of data: the initial questionnaire scores and the follow-up questionnaire

Circle one: Dependent Independent

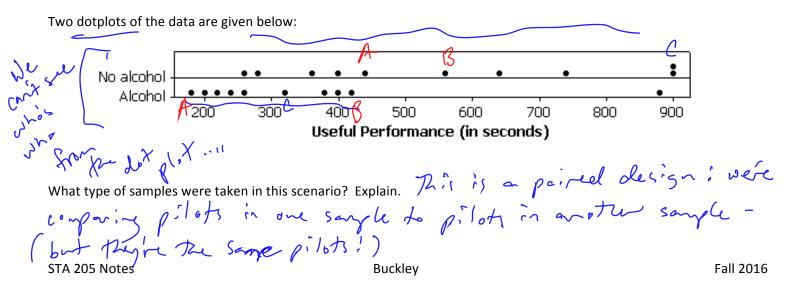
Explain: V' Leo is the treatment is the Sample of t

Example 2: Thirty dogs were selected at random from those residing at the humane society last month. The 30 dogs were split at random into two groups. The first group of 15 dogs was trained to perform a certain task using a reward method. The second group of 15 dogs was trained to perform the same task using a reward-punishment method. The investigator of this study will have two sets of data: the learning times for the dogs trained with the reward method and the learning times for the dogs trained with the reward-punishment method. Is this a paired or independent samples design?

Explain: The two sets unfilled of diss were unrelated - no attempt was made to fair a dos in one supple with a dos into

Inferences for Paired (Dependent) Samples

Example: Ten pilots performed tasks at a simulated altitude of 25,000 feet. Each pilot performed the tasks in a completely sober condition and, three days later, after drinking alcohol. At the completion of each simulation, the administrator recorded the time (in seconds) of useful performance of the tasks for each condition. The longer the pilot spends on useful performance, the better. The researchers would like to know if their useful performance decreases with alcohol use.



The data collected in the experiment is given below:

No alcohol	261	565	900	630	280	365	400	735	430	900	
Alcohol	185	375	310	240	215	420	405	205	255	875	
de NAI	-76	-190	-550	-390	-65	55	5	-530	-175	-25	

(only have 10 data points - so we should be a 1. #/o We can summarize the differences by calculating their sample mean and sample standard deviation in StatCrunch:

7 = -198,1 = d

Based on the sample data, can we conclude that useful performance decreases with alcohol use? Use α = 0.05. Note – the two-sided p-value for this test is 0.0227.

; Ha: Ma < O (affected performance) H.: Ma = 0

(2) d=,05; reject Remill in favor of Realtered

pd <0 if product &

t = d-Md = -198,1-0 = -2.71 / big.11"

tind-1 = 22x1.04

10222, Se A = p-value = .01135 < d (4) With a = . 05 we reject the mil of no difference in form of Md < 01 dicoll has a negative etter of promuee.

Formulas & Assumptions for Dependent (Paired) Samples Who he saylis we privad, then all informes are about differences (d) between the pairs, Create variable of = V2-V1 + the do the usual one scaple state (hypothesis tist or confidence intervals): T.S. called the standard en _ in Statement + statistics.

Example: An article in the New York Times compared the prices of some common food items at the Whole Food
Market and at Fairway Supermarket in New York City. Prices were determined for the same ten items (Half-gallon milk
64 oz. of orange juice, etc.) at each of the two stores. The data is available on StatCrunch.

Explain why the samples of prices are dependent samples. pained samples - 5 cm item compared in both stores, on price

Use the StatCrunch output below to estimate the mean difference in prices at the two stores with 90% confidence.

'			•					
90% confidence interval results:								
μ_1 - μ_2 : mean of the \textbf{PAIRED} difference between Fairway and Whole Foods								
Difference	Sample Diff.	Std. Err. DF	1 1					
Fairway - Whole Foods	-0.68	0.2076161 9	1.833 Kuit					

Were going to brited a 90% confidence interval for the mean difference Ma, d= Fairway-WF

-,68 ± 1.733 . SE + 1.737 · 0,2076 C.I. = (-1.06, -0,299)

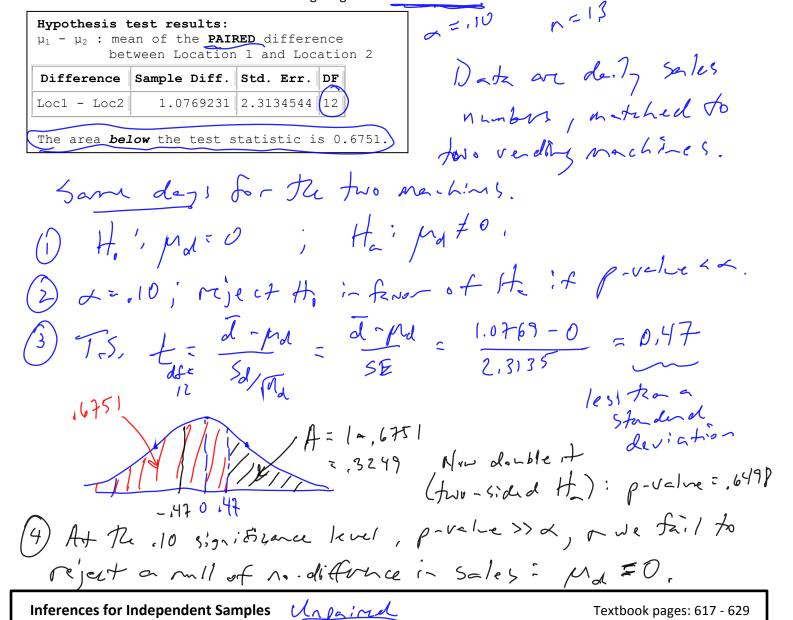
for the men difforme

So our conclusion is that My is negative - means that WF is nove expensit han Fairway. - with 70% a folace. (Small Saple size natur me nervous!)

What happens if the limits of the interval have different signs (ie: a negative lower limit & a positive upper limit)?

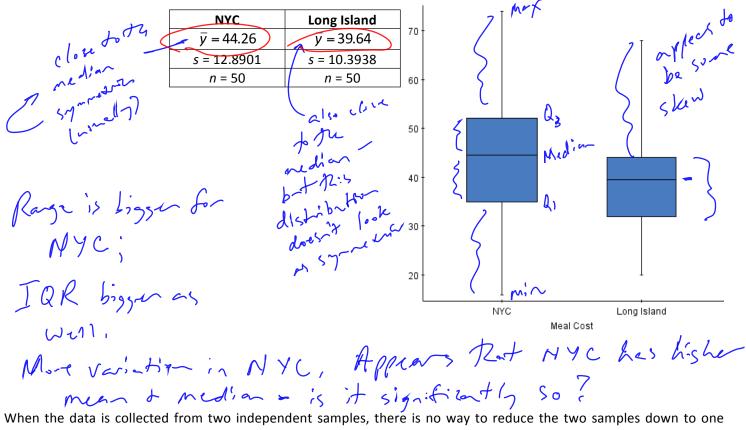
Ours didn't; but if instead we'd seen [-1.06, 0.299], then O would be a possibility - O is i-that interest, so it's possible 12-+ maso - i.e., Rois no differences in priver,

Example: A distributor of soft drinks knows from experience that the number of drinks purchased from a machine each day varies according to the location of the machine. At a school, two machines are placed in what the distributor believes to be two optimal locations. Both of the machines are observed for a random sample of 13 days, and the number of drinks sold each day is recorded. Using the output below, determine if there is a difference in the mean number of drinks sold at the two locations using a significance level of 0.10.



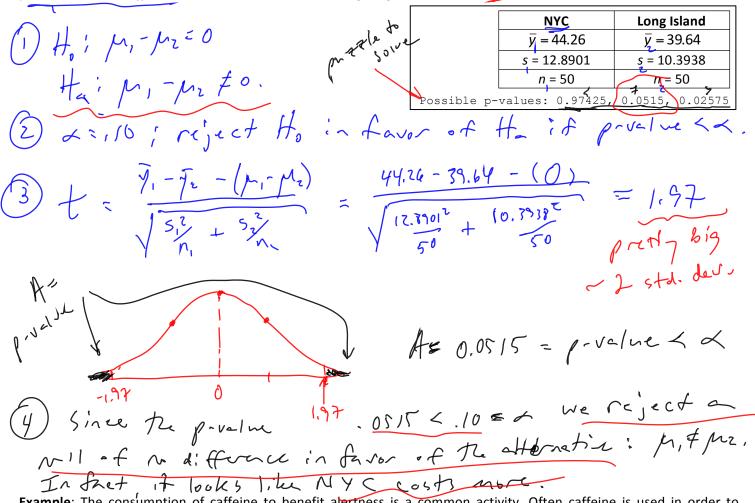
Example: A travel guide is interested in comparing the mean price per person for a meal in NYC and the mean price per person for a meal in Long Island restaurants. In order to do this, a random sample of 50 restaurants in NYC is selected and a random sample of 50 restaurants in Long Island is taken – the prices at these 100 restaurants are available on StatCrunch. At the 0.10 level, is there sufficient evidence to conclude the mean price per person for a meal differs between the two locations?

- Explain why the samples collected were independent. The obs. with - restaurants inter two locations - have noting to do with each other. They are unpaired. — Boxplots and summary statistics comparing the prices are shown below (an asterisk has been added to the boxplot denoting the mean). Compare and contrast the two distributions.



Formulas & Assumptions for Independent Samples Variable in any sailble way
We'll exercis parameters or statistics in terms of
Ho! M, - Mz = 0 Ha: M, -Mz { }
$ \begin{array}{c} (\text{or } M_1 = M_2) \\ (\sqrt{y_1 - y_2}) - (M_1 - M_2) \end{array} $ $ \begin{array}{c} N_1 \text{ from } N_2 \\ \sqrt{y_1 - y_2} \end{array} $
1.57, to Sin + Sin Standard error as Abefore.
C.I. $y_1 - y_2 = t_{(rit)} / \frac{5^2}{n_1} + \frac{5^2}{n_2}$

Back to the example: The following StatCrunch output was obtained. Use this to determine if the mean price per person for a meal differs between the two locations using a significance level of 0.10.



Example: The consumption of caffeine to benefit alertness is a common activity. Often caffeine is used in order to replace the need for sleep. One recent study was undertaken to determine if there was a difference in students' ability to recall memorized information after either the consumption of caffeine or a brief sleep. A random sample of 24 adults (between the ages of 18 and 39) were randomly divided into two groups of 12 participants each and verbally given a list of 24 words to memorize. During the break, one group takes a 90 minute nap while the other group is given a caffeine pill. After the break, each participant is asked to recall as many of the 24 words as possible. Researchers record the number of words each participant recalled.

Identify the variable recorded for this study. Classify the variable as categorical or quantitative.

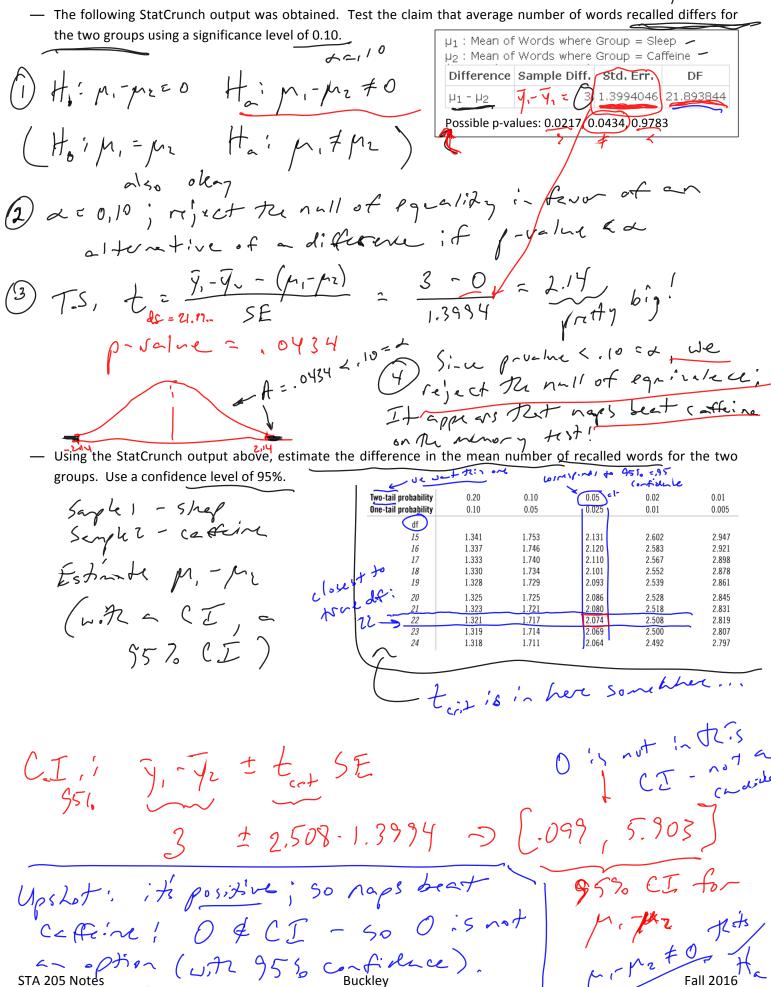
at of words recalled; quantitative

 Explain why the collected samples are independent. No connection made - no pairing - between indisidual observational units (i.e. students) in the two samples. No way of creating a reason, In I difference variable d. Buckley

STA 205 Notes

Ungained.

Fall 2016



Equality is not an often.

Example: Researchers speculate that drivers who do not wear a seatbelt are more likely to speed than drivers who do wear one. The following data were collected on a random sample of 20 drivers who were clocked to see how fast they were driving (mph).

7	_	Seatbelt	62	60	68	64	72	75	63	60	64	80	NI=10
\	\ _	No Seatbelt	72	85	72	62	84	76	66	63	65	64	nz=10
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What type of samples were selected - independent or dependent (paired)? Explain.

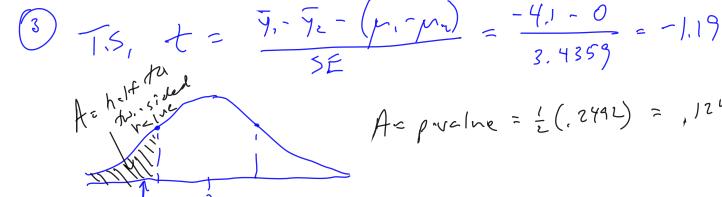
unpaired - There is no pairing attented between observations I with in the two sayles,

StatCrunch was used to analyze the data, and the output for both types of samples (independent and dependent) is given below. Using the appropriate output, determine if the mean speed is higher for those who do not wear seatbelts than for drivers that do at a significance level of 0.05.

Hypothesis test results: μ_1 : mean of Seatbelt μ_2 : mean of No seatbelt							
Difference	Sample Mean	Std. Err.	DF				
$\mu_1 - \mu_2$	-4.1	3.4359214	17.185564				
The two-sic	ded n-value i	s 0 2492					

Hypothesis test results:								
μ_1 - μ_2 : mean of Seatbelt and No s		ference bet	ween					
Difference	Sample Diff.	Std. Err.	DF					
Seatbelt - None	-4 1	3.3281627	9					
The two-sided p-v	alue is 0.2632.							

Ho: M,-Mz =0 Hi: M,-Mz <0 (M, </12) 2) da, 05; reject a null of no differe en favor of the attention of mon-sect bett drives drive faster it Revalue < 1



A= proline = {(,2492) = ,1246 70

Since the presalue is greater than I, we fail to reject a mill of equality: as far as we can till, there STA 205 Notes is no significant Buckley difference in speeds, Fall 2016