Packet 7: Summarizing Quantitative Data

After completing this material, you should be able to:

- describe the distribution of a quantitative variable by discussing its shape, center, spread, and unusual characteristics.
- calculate (using StatCrunch) measures of center and measures of spread.
- apply the Empirical Rule or Chebyshev's Rule to a distribution when discussing the standard deviation.
- compare distributions using boxplots.

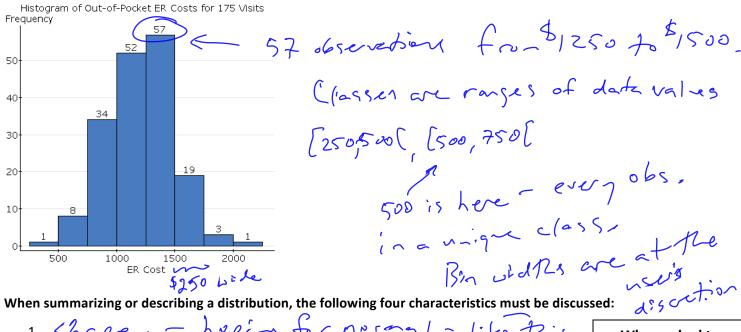
Recall: What is a quantitative variable?

Messeres a variable using real numbers.

To summarize a quantitative variable, we need a new graphical display – a bar graph cannot be used. We will first look at histograms for graphically summarizing quantitative data. What exactly is a histogram?

The numeric values are decided into no-noverlapping classes (or bins) that span all the dorta, or every observation is in one only one class

Example: Money magazine undertook a study in 2009 to estimate the average cost for a visit to a hospital emergency room. A random sample of 175 emergency room visits in a certain urban area was taken, and the out-of-pocket costs associated with that visit were recorded. A histogram for the collected data is given below:



1. Shape - hoping for normal - like tais مرو [2. center - typical velmes

3. Sprad - Summarizes the varieti's 1.2 y in

4. offiers - odd or extreme values; we worry about nistales or data errors.

When asked to describe a distribution, make sure you address these four characteristics in context and in complete sentences.

Textbook pages: 48 – 50; 53 – 72

Shape of the distribution

When describing a distribution, the first think we should consider is what shape the distribution has. We will consider **five** common shapes (shown below):

Shape	Histogram	Description
$\mathcal{M}_{\mathcal{I}}$	Normal Dist.	A symmetric, uni- nod-1 distribution.
	One mode or hump	
	Bi-nodal Dist	Maybe tere are two different types of
Mille		different types of
-1111HIII	("fro moder")	obs. with
	Uniform Dist	A symmetric dist.
MIMMIM	(sere heights)	w/o a side - de si of
Th ~	Slewed Riszt	Like a Z2 for example
Milhon	(fillow the tail	Long tail to the right
,	Shewed Left	

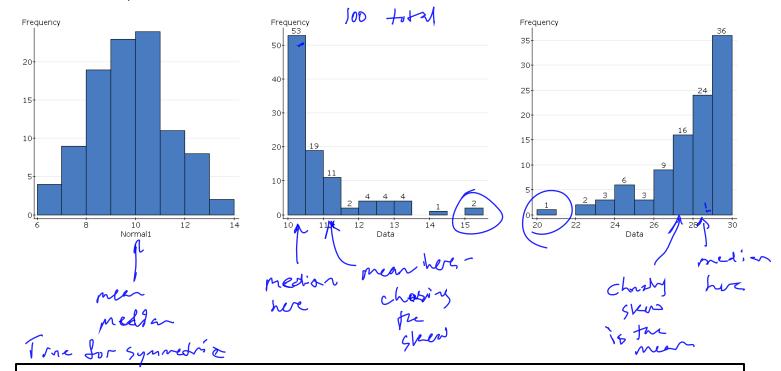
Measures of Center

Once we know the shape of a distribution, it is common to summarize it by finding a "typical" value of the distribution – these values are generally referred to as measures of center. There are two common measures of center which are used:

Measure of Center	Notation	Description
mean - averge	m-p-p-	Remmer'in a every of the
(chaves the skew)	y - sample	data - Sers. For to skew
	(O_	Re value such that half
meden - middle Value of (sorted) doon	(non standard)	are before + hilf are above.

The calculation of these measures, while not difficult, can be tedious. Instead of calculating these summary statistics by hand, we will rely on the use of StatCrunch.

How does the shape of the distribution affect measures of center?



Measures of Spread

Unfortunately, a measure of center doesn't adequately describe a distribution. We also must have some idea how the values in the distribution vary. This requires a measure of spread. There are three common measures of spread which are used:

Measure of Spread	Notation	Description
Range	non Spanded	The distance between max and min. 1008 of data within that som.
Intra-rhl- range	IQR = Q - R1 2	Re distance between Re middle 50% of data - Range of middle 50%,
Standard deviation	5 - Souple std. dev.	Typical deviation - monprising deviation - from Remean.

The calculation of these measures can be quite difficult – the formula for standard deviation is quite tedious. Instead of calculating these summary statistics by hand, we will rely on the use of StatCrunch.

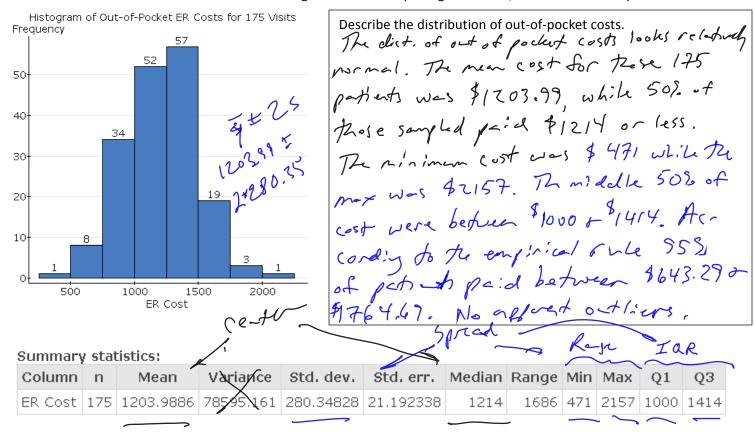
be aware of Puse

Unusual Observations Ontliers, -> risk skewing tings.

Unusual observations are often referred to as *outliers*. When determining if unusual observations are present in the data, look for observations which do not follow the overall patter of the data. These will generally be observations which are in the tail of the distribution – either very large or very small.

STA 205 Notes When are they ceal Buckley or in error? These Fall 2016

Example: Money magazine undertook a study in 2009 to estimate the average cost for a visit to a hospital emergency room. A random sample of 175 emergency room visits in a certain urban area was taken, and the out-of-pocket costs associated with that visit were recorded. A histogram for the sample is given below, as well as summary statistics:



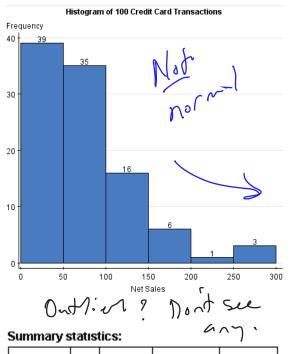
How can the standard deviation be interpreted?

Empirical Rule	p + 1.00
6 8% between	y± s
952 "	M± 70
99.7% "	m = 38

works for all!

Chebyshev's Rule	che works for all
disdibe	
at 75%.	betreen ? stel- der. from the mean on \$ 20
1 902	M=30
1255	o o ve fr

Example: Pelican Stores, a division of National Clothing, is a chain of women's apparel stores operating throughout the country. The chain recently sampled 100 in-store credit transactions in order to gain insight about the spending habits of their customers. A histogram of these transactions is given below, as well as various summary statistics:



Column	n	Mean	Variance	Std. Dev.
Net Sales	100	77.6005	3098.5854	55.66494

Median	Range	Min	Max	Q1	Q3
59.705	274.36	13.23	287.59	39.6	101.4
				$\overline{}$	_

The distribution of <u>credit</u> card seles has a
shape that is 4 kerred right. The average purchase
in this sample of 100 transactions is 477.60
and 50% of the transactions have an amount of
$\frac{\cancel{\cancel{4}}\cancel{\cancel{59.71}}}{\cancel{\cancel{59.71}}}$ or less. The minimum purchase was
$\frac{4}{13,73}$, while the maximum was
$\frac{4}{13.73}$, while the maximum was $\frac{1}{287.59}$. The middle $\frac{50}{\%}$ of purchases in
this sample were between \$39.60 and $\frac{$101.40}{}$.
According to Cheby shevis Rule, we expect
25 % of purchases at this store to fall between
\$0 and \$188.93
(two standard deviations from the mean).

77.60 ± 24 55.66 left side is nightim! So put 0 to tre left

Comparing Distributions

Generally, we can answer much more interesting questions when we compare two or more distributions. It can be cumbersome to compare several different histograms, so a different graphical display called a boxplot is often used. A boxplot is based on the 5-number summary which consists of the following five staitsitcs:









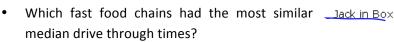


Textbook pages: 88 - 95

These statistics are then used to construct a boxplot. A generic boxplot is shown below:



Example: A large number of fast-food restaurants with drive-through windows offer drivers and their passengers the advantages of quick service. To measure the quality of service, an organization called QSR planned a study in which the amount of time taken by a sample of drive-through customers at each of five restaurants (Popeye's, Wendy's, McDonald's, Hardee's, and Jack in the Box) was recorde 'Restaurant's Restaurant's Restaurant's Restaurant's Restaurant's Restaurant Restaur



M+H; H+P; M+W

 Which fast food chain has a distribution of drive thru times that is likely right skewed?

McDonalds

Wendys

Popeyes

100

150

200

250

Service time (seconds)

 Which fast food chain had the smallest innerquartile range of drive through times?

Which are asymmetric?

Werdys

• Which fast food chain had the most variability according to their ranges?

Hadre

(Biggest range)

• Which fast food chain was responsible for the overall fastest service in the sample? Which was responsible for the overall slowest service?

Wedge Wins on almost every neasure - smallest non " nex " nedian

(We receive no funding or food from Wendys)